

Choose 3 of the following identities in each section and verify. Choose any additional problem from any level. You should complete a total of 10 problems. Show all work.

**Level 1**

1.  $\csc\theta\cos\theta = \cot\theta$

2.  $(\sec\beta - 1)(\sec\beta + 1) = \tan^2\beta$

3.  $\tan\phi\cot\phi - \cos^2\phi = \sin^2\phi$

4.  $\cos^2\theta(1 + \tan^2\theta) = 1$

5.  $3\sin^2 + 4\cos^2x = 3 + \cos^2x$

6.  $(\sec\alpha + \tan\alpha)(\sec\alpha - \tan\alpha) = 1$

**Level 2**

7.  $(\sin\theta + \cos\theta)^2 + (\sin\theta - \cos\theta)^2 = 2$

8.  $1 - \frac{\cos^2x}{1+\sin x} = \sin x$

9.  $\frac{1+\sin\theta}{1-\sin\theta} = \frac{\csc\theta+1}{\csc\theta-1}$

10.  $\frac{\sec x}{\csc x} + \frac{\sin x}{\cos x} = 2\tan x$

11.  $1 - \frac{\sin^2x}{1+\cos x} = \cos x$

12.  $\sin\mu(\cot\mu + \tan\mu) = \sec\mu$

**Level 3**

13.  $\tan\alpha + \cot\alpha - \sec\alpha\csc\alpha = 0$

14.  $\frac{\sec\theta - \csc\theta}{\sec\theta\csc\theta} = \sin\theta - \cos\theta$

15.  $\tan x = \sin x \sec x$

16.  $\tan^2\alpha\cos^2\alpha + \cot^2\alpha\sin^2\alpha = 1$

17.  $\frac{\cos x}{1+\sin x} + \frac{1+\sin x}{\cos x} = 2\sec x$

18.  $\frac{(\sec\sigma - \tan\sigma)^2 + 1}{\csc\sigma(\sec\sigma - \tan\sigma)} = 2\tan\sigma$

Solve each equation in the interval  $[0, 2\pi)$ . Show all work. Circle the answers.

1.  $2\sin x - 1 = 0$

2.  $\sqrt{3}\sec x - 1 = 0$

3.  $3\tan^3 x = \tan x$

4.  $2\sin^2 x + 3\sin x + 1 = 0$

5.  $\csc x - 2 = 0$

6.  $\csc x + \cot x = 1$

7.  $(3\tan^2 x - 1)(\tan^2 x - 3) = 0$

8.  $\sec x \csc x = 2\csc x$

Find the value using the sum, difference, or double angle identities.

9.  $\sin u = -\frac{4}{5}$ ,  $\pi < u < \frac{3\pi}{2}$ , find  $\cos 2u$ .

10.  $\cos u = -\frac{2}{3}$ ,  $\frac{\pi}{2} < u < \pi$ ;  $\sin v = \frac{4}{5}$ ,  $0 \leq v \leq \frac{\pi}{2}$ , find  $\sin(u - v)$ .

11.  $\tan u = \frac{3}{4}$ ,  $0 < u < \frac{\pi}{2}$ ;  $\cos v = -\frac{4}{5}$ ,  $\frac{\pi}{2} \leq v \leq \frac{3\pi}{2}$ , find  $\sin(u + v)$  and  $\cos(u - v)$ .

Use the sum, difference, or double angle identities to find the following values.

12.  $\cos^{-1}105^\circ$ .

13.  $\sin 195^\circ$ .

14.  $\cos 255^\circ$ .

15.  $\sin^{-1}285^\circ$ .