

TWO COLUMN PROOFS OF TRIG IDENTITIES

Listed below are proofs of trigonometric identities. It is your job to determine the theorem, property, or identity used in each step. (Think of this as a two-column proof similar to the ones you LOVED to do in Geometry.) Not all steps will have trig reasons.

| Proof | Reason |
|---|--|
| $\sin x + \cos x = \frac{\cot x + 1}{\csc x}$ $= (\cot x + 1) \csc x$ $= (\cot x + 1) \cdot \frac{1}{\csc x}$ $= (\cot x + 1) \cdot \sin x$ $= \cot x \sin x + \sin x$ $= \frac{\cos x}{\sin x} \sin x + \sin x$ $= \cos x + \sin x$ | <p>Given</p> <p>Division</p> <p>mult by reciprocal</p> <p>rewrite</p> <p>distribute</p> <p>rewrite</p> <p>simplify</p> |
| <p>2.</p> $\frac{1}{\sec x - \tan x} = \sec x + \tan x$ $\frac{1}{\sec x - \tan x} \cdot \frac{\sec x + \tan x}{\sec x + \tan x} =$ $\frac{\sec x + \tan x}{\sec^2 x - \tan^2 x} =$ $\frac{\sec x + \tan x}{1 + \tan^2 x - \tan^2 x} =$ $\sec x + \tan x =$ | <p>Reason</p> <p>Given</p> <p>mult by conjugate</p> <p>multiply</p> <p>Pythagorean ID</p> <p>simplify</p> |

3. Proof

Reason

$$\frac{\sec^2 x - 1}{\sec^2 x} = \sin^2 x$$

$$\frac{\sec^2 x}{\sec^2 x} - \frac{1}{\sec^2 x} =$$

$$1 - \frac{1}{\sec^2 x} =$$

$$1 - \cos^2 x =$$

$$\sin^2 x + \cos^2 x - \cos^2 x =$$

$$\sin^2 x =$$

Given

split fraction

simplify

rewrite

Pythagorean ID

simplify

Proof

Reason

$$2 \sec x = \frac{1 + \sin x}{\cos x} + \frac{\cos x}{1 + \sin x}$$

$$= \frac{(1 + \sin x)^2}{\cos x(1 + \sin x)} + \frac{\cos^2 x}{\cos x(1 + \sin x)}$$

$$= \frac{1 + 2\sin x + \sin^2 x}{\cos x(1 + \sin x)} + \frac{\cos^2 x}{\cos x(1 + \sin x)}$$

$$= \frac{1 + 2\sin x + \sin^2 x + \cos^2 x}{\cos x(1 + \sin x)}$$

$$= \frac{1 + 2\sin x + 1}{\cos x(1 + \sin x)}$$

$$= \frac{2 + 2\sin x}{\cos x(1 + \sin x)}$$

$$= \frac{2(1 + \sin x)}{\cos x(1 + \sin x)}$$

$$= \frac{2}{\cos x}$$

$$= 2 \cdot \frac{1}{\cos x}$$

$$= 2 \sec x$$

Given

Common denominators

multiply

add fractions

Pythagorean ID

combine like terms

GCF

simplify

rewrite

rewrite