

$$\begin{bmatrix} 2 & 3 \\ -1 & 0 \end{bmatrix} Y = \begin{bmatrix} 3 \\ 2 \\ 5 \end{bmatrix}$$

Inverse ↓

$$\therefore \begin{vmatrix} 2 & 3 \\ -1 & 0 \end{vmatrix} = 2(0) - (-1)(3) \\ = 0 - -3 \\ = 3$$

$$\frac{1}{|A|} \begin{bmatrix} d & -b \\ -c & a \end{bmatrix}$$

$$Y = \frac{1}{3} \begin{bmatrix} 0 & -3 \\ 1 & 2 \end{bmatrix} \begin{bmatrix} 3 & -1 \\ 2 & 5 \end{bmatrix}$$

$2 \times 2 \quad 2 \times 2$

$$\begin{bmatrix} 0(3) + (-3)(2) & 0(-1) + (-3)(5) \\ 1(3) + 2(2) & 1(-1) + 2(5) \\ 3 + -6 & -1 + -15 \\ 7 & 9 \end{bmatrix}$$

$$= \frac{1}{3} \begin{bmatrix} -6 & -15 \\ 7 & 9 \end{bmatrix}$$

$$Y = \begin{bmatrix} -2 & -5 \\ \frac{7}{3} & 3 \end{bmatrix}$$

$$\begin{bmatrix} 2 & 3 \\ -1 & 0 \end{bmatrix} Y = \begin{bmatrix} 3 \\ 2 \end{bmatrix}$$

$$D = \begin{vmatrix} 2 & 3 \\ -1 & 0 \end{vmatrix} = 2(0) - (-1)(3) = 3$$

$$x = \frac{D_x}{D} = \frac{-6}{3} = -2$$

$$D_x = \begin{vmatrix} 3 & 3 \\ 2 & 0 \end{vmatrix} = 3(0) - 2(3) = -6$$

$$y = \frac{D_y}{D} = \frac{7}{3} = \frac{7}{3}$$

$$D_y = \begin{vmatrix} 2 & 3 \\ -1 & 2 \end{vmatrix} = 2(2) - (-1)(3) = 4 + 3 = 7$$

Warm-up

January 27, 2017

Solve .

$$\begin{bmatrix} 3 & 2 \\ -1 & 0 \end{bmatrix} X = \begin{bmatrix} 2 & 3 \\ -1 & 0 \end{bmatrix}$$

$$\frac{1}{2} \begin{bmatrix} 2 & 0 \\ 1 & 3 \end{bmatrix}$$

$$0 - -2 = 2$$

before

$$\begin{bmatrix} 0 & -a \\ 1 & 3 \end{bmatrix}$$

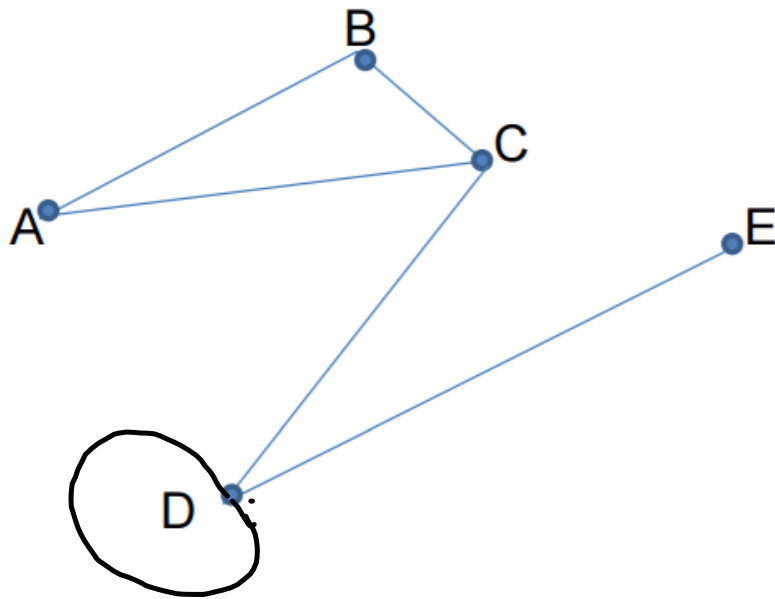
$a \times a$

$$\begin{bmatrix} 2 & 3 \\ -1 & 0 \end{bmatrix}$$

$a \times a$

$$\begin{bmatrix} 2 & 0 \\ 1 & 3 \end{bmatrix}$$

$a \times a$



vertex-edge
graph

$$\begin{matrix} & & A & B & C & D & E \\ \begin{matrix} A \\ B \\ C \\ D \\ E \end{matrix} & \begin{bmatrix} 0 & 1 & 1 & 0 & 0 \\ 1 & 0 & 1 & 0 & 0 \\ 1 & 1 & 0 & 1 & 0 \\ 0 & 0 & 1 & 1 & 1 \\ 0 & 0 & 0 & 1 & 0 \end{bmatrix} \end{matrix}$$

adjacency
matrix

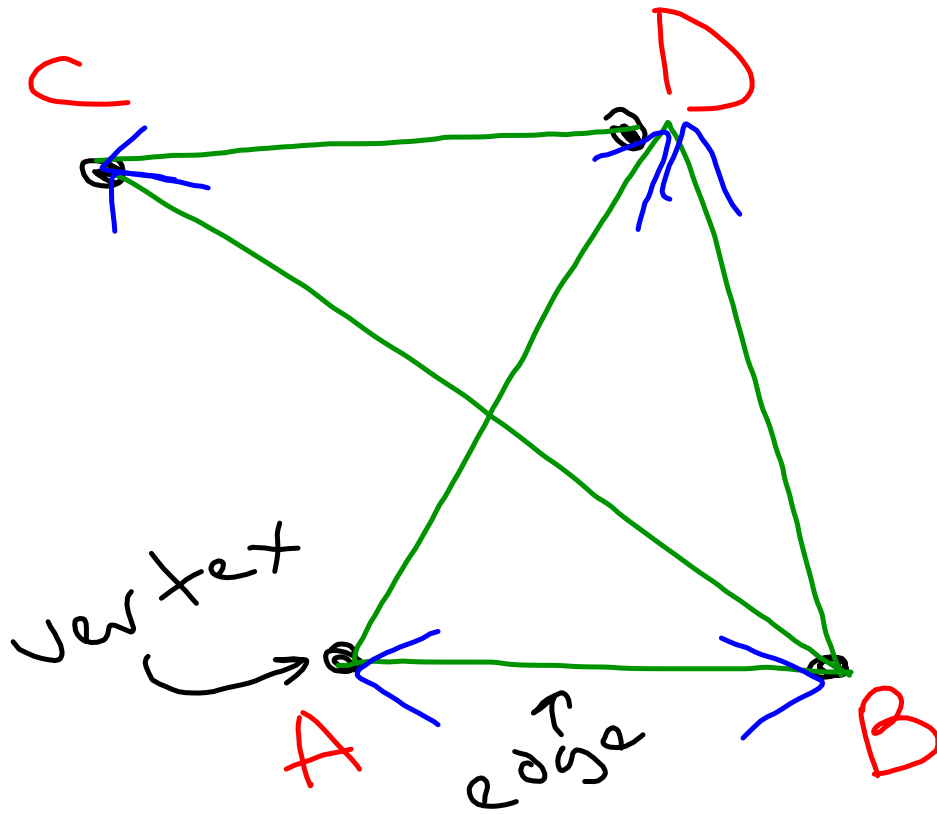
$$\begin{matrix} F & D & C & B & D \\ \left[\begin{array}{cccccc} 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 1 & 0 \end{array} \right] \end{matrix}$$

adjacency
matrix

5×5

	A	B	C	D	E
A	0	1	1	0	0
B	1	0	1	0	0
C	1	1	0	1	0
D	0	0	1	1	1
E	0	0	0	1	0

Adjacency Matrix



vertex-edge graph
digraph

$$\begin{matrix} D & C & B & A \\ \left[\begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{array} \right] \end{matrix}$$

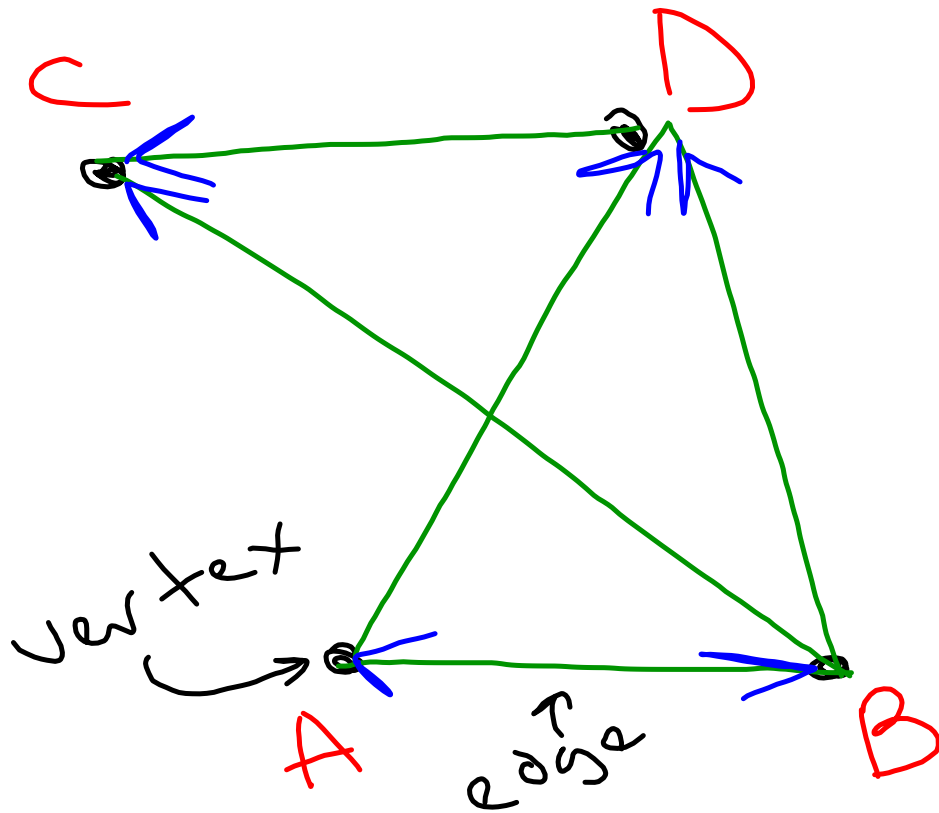
$$\begin{matrix} D & C & B & A \\ \left[\begin{array}{cccc} 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{array} \right] \end{matrix}$$

$$\begin{matrix}
 & A & B & C & D \\
 D & 1 & 1 & 1 & 1 \\
 C & 0 & 1 & 0 & 1 \\
 B & 1 & 0 & 1 & 1 \\
 A & 0 & 0 & 0 & 1
 \end{matrix}$$

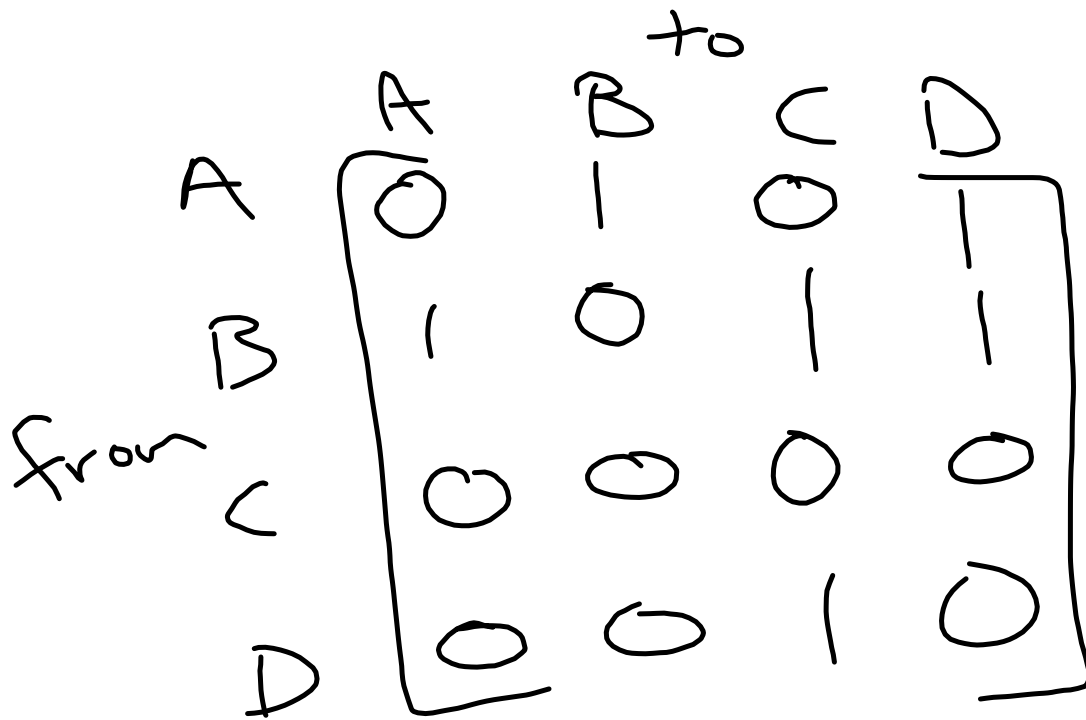
from

$$\begin{matrix}
 & A & B & C & D \\
 D & 0 & 0 & 0 & 0 \\
 C & 0 & 0 & 0 & 0 \\
 B & 1 & 0 & 0 & 0 \\
 A & 0 & 1 & 1 & 1
 \end{matrix}$$

to

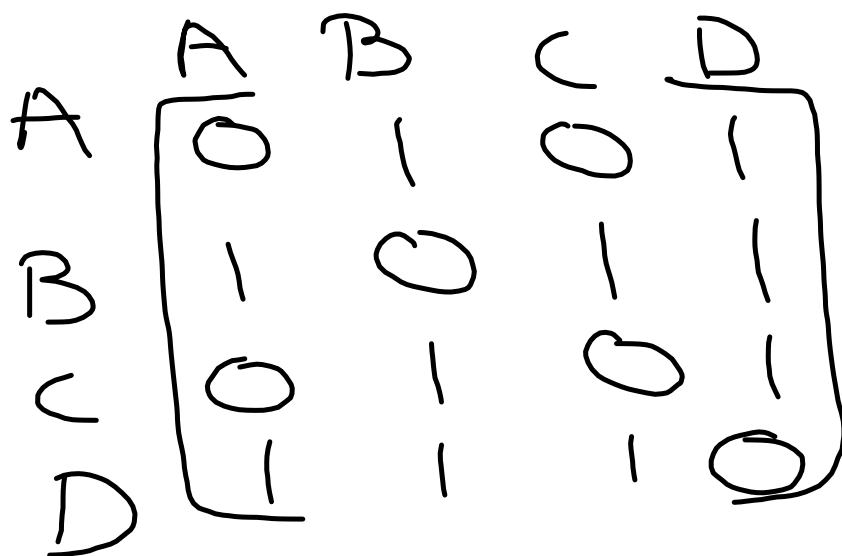


digraph
↓
direction



digraph

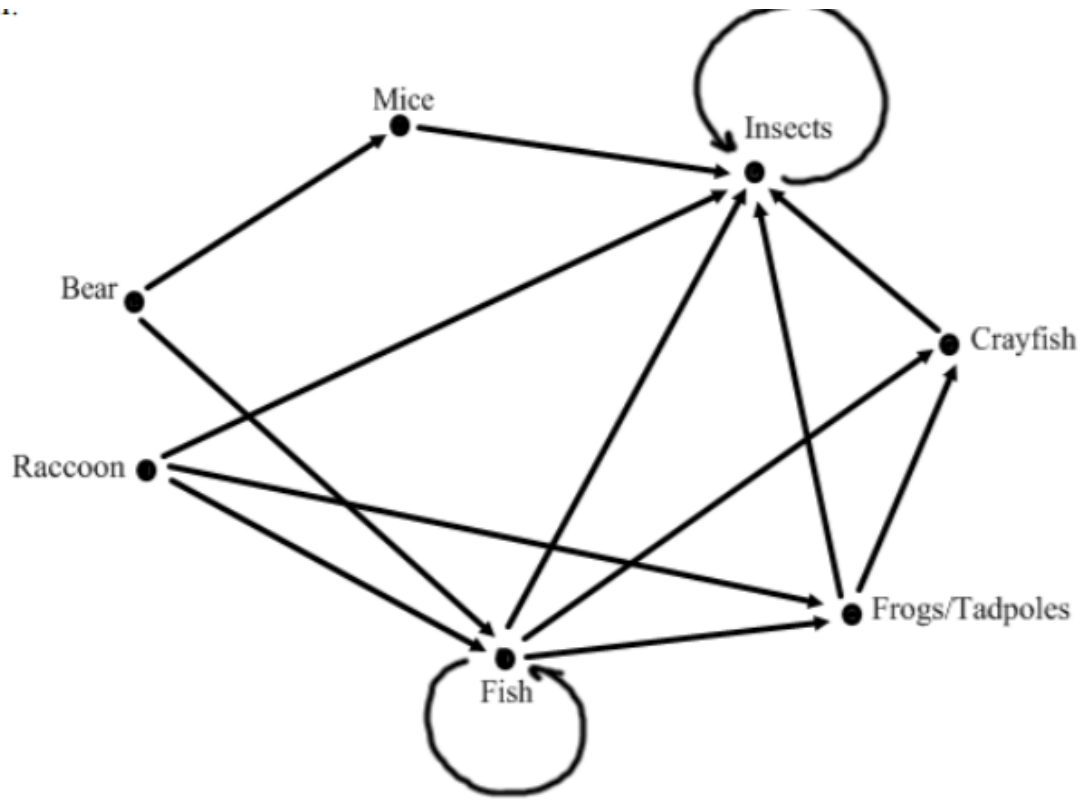
Adjacency matrix



vertex-edge

adjacency matrix

from.



$$\begin{matrix} & B & C & F & F_r & I & M & R \\ \begin{matrix} B \\ C \\ F \\ F_r \\ I \\ M \\ R \end{matrix} & \begin{bmatrix} 0 & 0 & 1 & 0 & 0 & 1 & 0 \end{bmatrix} \end{matrix}$$

$$\begin{matrix} & B & C & F & F_r & I & M & R \\ \begin{matrix} B \\ C \\ F \\ F_r \\ I \\ M \\ R \end{matrix} & \begin{bmatrix} 0 & 0 & 1 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 1 & 1 & 1 & 1 & 0 & 0 \\ 0 & 1 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 & 1 & 0 & 0 \end{bmatrix} \end{matrix}$$

	B	C	F	F _r	I	M	R
B	0	0	1	0	0	1	0
C	0	0	0	0	1	0	0
F	0	1	1	1	1	0	0
F _r	0	1	0	0	1	0	0
I	0	0	0	0	1	0	0
M	0	0	0	0	1	0	0
R	0	0	1	1	1	0	0

De'v