

Double- and Half-Angle Identities

Use a double-angle identity to find the exact value of each expression.

1) $\sin 120^\circ$

2) $\tan 60^\circ$

3) $\cos \frac{4\pi}{3}$

4) $\sin \frac{5\pi}{3}$

Use a half-angle identity to find the exact value of each expression.

5) $\tan 45^\circ$

6) $\sin 165^\circ$

7) $\sin \frac{5\pi}{6}$

8) $\cos 30^\circ$

9. Find the exact value of each of the following under the given conditions: $\sin u = \frac{3}{5}$, $\frac{\pi}{2} < u < \pi$

$$\tan v = \frac{5}{12}, \quad \pi < v < \frac{3\pi}{2}$$

A. $\sin(u+v)$

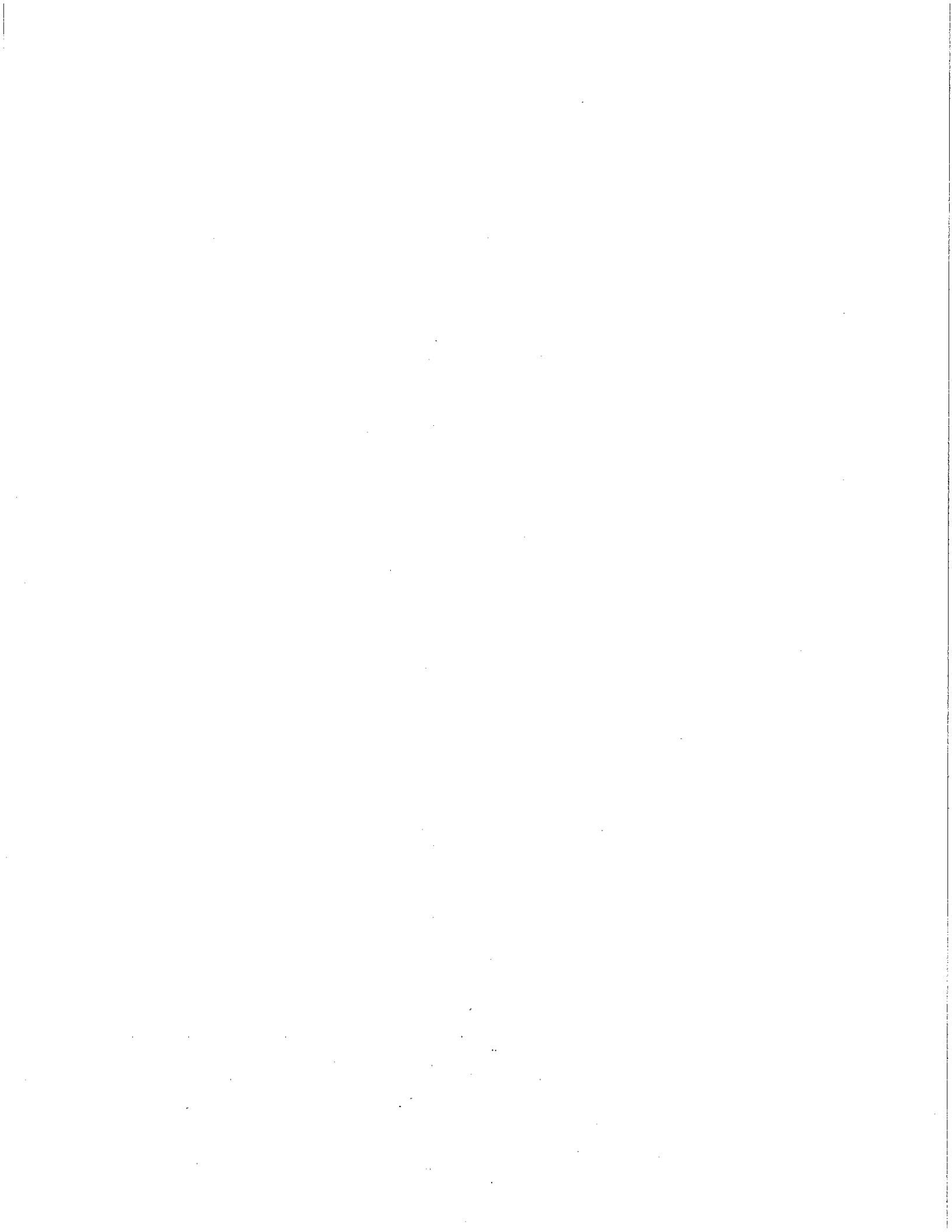
B. $\cos(u+v)$

$$\sin u = \frac{-4}{5}, \quad \pi < u < \frac{3\pi}{2}$$

$$\text{and } \cos v = \frac{3}{5}, \quad 0 < v < \frac{\pi}{2}$$

C. $\cos(u+v)$

D. $\sin(u-v)$



15) $\sin \theta = -\frac{7}{25}$ and $270^\circ < \theta < 360^\circ$

Find $\cos \frac{\theta}{2}$

17) $\cos \theta = \frac{4}{5}$ and $270^\circ < \theta < 360^\circ$

Find $\sin 2\theta$

19) $\cos \theta = -\frac{4}{5}$ and $90^\circ < \theta < 180^\circ$

Find $\sin \frac{\theta}{2}$

21) $\tan \theta = -\frac{7}{24}$ and $\frac{3\pi}{2} < \theta < 2\pi$

Find $\cos \frac{\theta}{2}$

23) $\cot \theta = \frac{4}{3}$ and $\pi < \theta < \frac{3\pi}{2}$

Find $\cos 2\theta$

25) $\sin \theta = -\frac{3}{5}$ and $\frac{3\pi}{2} < \theta < 2\pi$

Find $\tan \frac{\theta}{2}$

16) $\sin \theta = \frac{1}{3}$ and $0^\circ < \theta < 90^\circ$

Find $\cos 2\theta$

18) $\cos \theta = \frac{2\sqrt{5}}{5}$ and $0^\circ < \theta < 90^\circ$

Find $\sin \frac{\theta}{2}$

20) $\cos \theta = -\frac{15}{17}$ and $180^\circ < \theta < 270^\circ$

Find $\tan \frac{\theta}{2}$

22) $\cot \theta = \frac{4}{3}$ and $\pi < \theta < \frac{3\pi}{2}$

Find $\sin 2\theta$

24) $\tan \theta = 2$ and $0 < \theta < \frac{\pi}{2}$

Find $\sin \frac{\theta}{2}$

26) $\cot \theta = -\frac{3\sqrt{91}}{91}$ and $\frac{3\pi}{2} < \theta < 2\pi$

Find $\sin \frac{\theta}{2}$

