## Algebra 1

## Unit 2 Part 3

## Quadratic Functions

|  |  |  | Thursday, March $11^{\text {th }}$ | Friday, <br> March $12^{\text {th }}$ |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  | Transformations of Quadratic Functions | Graphing in Vertex Form Characteristics |
| Monday, March $15^{\text {th }}$ | Tuesday, March $16^{\text {th }}$ | Wednesday, March 17 ${ }^{\text {th }}$ | Thursday, March $18^{\text {th }}$ | Friday, <br> March 19 ${ }^{\text {th }}$ |
| Graphing in Standard Form Characteristics | Graphing Characteristics Quiz Opens at 3:30 PM | Converting Between Vertex Form and Standard Form <br> Quiz Due By Midnight | Quadratic Word Problems |  |
| Monday, March $22^{\text {nd }}$ | Tuesday, March 23rd | Wednesday, <br> March $24^{\text {th }}$ | Thursday, March $25^{\text {th }}$ | Friday, <br> March $26^{\text {th }}$ |
| Quadratic Word Problems | Review | Unit 2 Part 3 Test (during class) |  |  |

## Transformations of Quadratic Functions Notes

The parent function of a function is the simplest form of a function. The parent function for a quadratic function is $\mathbf{y}=\mathbf{x}^{\mathbf{2}}$ or $\mathbf{f}(\mathbf{x})=\mathbf{x}^{\mathbf{2}}$. Complete the table and graph the parent function below.

| $\mathbf{x}$ | $\mathbf{x}^{2}$ |
| :---: | :---: |
| -3 |  |
| -2 |  |
| -1 |  |
| 0 |  |
| 1 |  |
| 2 |  |
| 3 |  |



As you can see, the graph of a quadratic function looks very different from the graph of a linear function.

The U-shaped graph of a quadratic function is called a $\qquad$ .

The highest/lowest point (or turning point) on a parabola is called the $\qquad$ .
Remember, in order for a function to be a quadratic function, one term must have $\qquad$ .

The graph above is our parent function - it represents a quadratic function that has not been changed in any way. We are going to talk about the transformations of quadratic functions and how those transformations are represented in the equation of a quadratic function.

## Exploring the " k "

Answer the following questions about the transformation from the parent graph (solid graph)to the new function (dotted parabola).


Describe the transformation:
What is the vertex of the new function?


Describe the transformation:
What is the vertex of the new function?

## Exploring the " h " Value

Answer the following questions about the transformation from the parent graph (solid graph) to the new function (dotted parabola).


Describe the transformation:
What is the vertex of the new function?


Describe the transformation:
What is the vertex of the new function?

## Exploring the " $a$ " Value

Answer the following questions about the transformation from the parent graph (solid graph) to the new function (dotted parabola).


Describe the transformation:
What is the vertex of the new function?


Describe the transformation:
What is the vertex of the new function?


Describe the transformation:
What is the vertex of the new function?

## Summary

Vertex Form:

| Variable | Summary of the Effects of the Transformations |  |  |
| :---: | :---: | :---: | :---: | :---: |
| a |  |  |  |
|  |  |  |  |
| $h$ |  |  |  |
|  |  |  |  |
| $k$ |  |  |  |

vertex: $\qquad$
Practice

1) Given the equations below, describe the transformations from the parent function and name the vertex:
a. $y=-(x-4)^{2}+7$
b. $y=-2(x+2)^{2}+5$
c. $y=\frac{1}{2}(x-3)^{2}-8$
2) Create an equation to represent the following transformations:
a. Shifted down 4 units, right 1 unit, and reflected across the $x$-axis
b. Shifted up 6 units, reflected across the $x$-axis, and stretch by a factor of 3
c. Shifted up 2 units, left 4 units, reflected across the $x$-axis, and shrunk by a factor of $3 / 4$.

Identifying Transformations Practice

| Equation | a, h, k values | Reflection? | Vertical Stretch or Shrink? | Horizontal Translation? | Vertical Translation? |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $y=-2 x^{2}+4$ |  |  |  |  |  |
| $y=\frac{3}{2}(x+1)^{2}$ |  |  |  |  |  |
| $y=\frac{1}{4}(x-2)^{2}-5$ |  |  |  |  |  |
| $y=-0.4 x^{2}$ |  |  |  |  |  |
| $y=\frac{2}{3}(x-3)^{2}+4$ |  |  |  |  |  |
| $y=4 x^{2}-2$ |  |  |  |  |  |
| $y=(x+1)^{2}-5$ |  |  |  |  |  |
| $y=-3(x-4)^{2}+1$ |  |  |  |  |  |
| $y=\frac{1}{2} x^{2}$ |  |  |  |  |  |
| $y=2(x+3)^{2}$ |  |  |  |  |  |
| $y=x^{2}+4$ |  |  |  |  |  |
| $y=(x+4)^{2}$ |  |  |  |  |  |
| $y=1.5 x^{2}-9$ |  |  |  |  |  |
| $y=-x^{2}+2$ |  |  |  |  |  |
| $y=-0.8(x-4)^{2}$ |  |  |  |  |  |
| $y=-3.2 x^{2}+11$ |  |  |  |  |  |

## Writing Equations in Vertex Form Practice

Write the equation for a quadratic function which has been...

1) reflected across the x-axis and translated down 3 units.
2) vertically stretched by a factor of 2 , and translated right 5 units.
3) reflected across the x-axis, vertically stretched by a factor of 1.5 , and translated left 1 unit.
4) vertically shrunk by a factor of $1 / 2$, translated right 2 units, and translated down 4 units.
5) translated left 3 units, reflected across $x$-axis, and translated up 2 units.
6) translated down 1 unit, translated right 7 units, and vertically shrunk by a factor of 0.3.
7) vertically stretched by a factor of 2.5, translated right 1.5 units, translated up 3.3 units, and reflected across the x-axis.
8) translated left 6 units, translated down 2 units, and reflected across the $x$-axis.
9) neither stretched nor shrunk but has a vertex at $(3,4)$.

## Transformations of Quadratic Functions - Matching

1) ___ Up 4 and left 2
2) ___ Reflect across $x$-axis and up 3
3) ___ Vertical stretch by 3 and right 5
4) ___ Vertical shrink by $\frac{1}{3}$ and right 5
5) ___ Right 2 and up 4
6) $\qquad$ Vertical stretch by 3 and down 5
7) ___ Reflect across $x$-axis and down 3
8) ___ Vertical shrink of $\frac{1}{3}$ and down 5
9) $\qquad$ Up 4 and right $\frac{1}{2}$
10) 


11) $\qquad$ Vertical stretch of 2, right 4 and up 3
12) $\qquad$ Reflect across x-axis, vertical stretch of 3 and left 5
13) __ Vertical shrink by $\frac{1}{2}$, right 2 and up 4
14) ___ Vertical shrink by $\frac{1}{2}$ and up 4
15) $\qquad$ Vertical stretch of 2 , left 3 and up 4
k. $f(x)=-x^{2}+3$
m. $f(x)=2(x+3)^{2}+4$
a. $f(x)=(x-2)^{2}+4$
b. $f(x)=-3(x+5)^{2}$
c. $f(x)=\frac{1}{2}(x-2)^{2}+4$
d. $f(x)=-(x+3)^{2}$
e. $f(x)=\frac{1}{3} x^{2}-5$
f. $f(x)=-x^{2}-3$
g. $f(x)=\left(x-\frac{1}{2}\right)^{2}+4$
h. $f(x)=\frac{1}{2} x^{2}+4$
i. $f(x)=3(x-5)^{2}$
j. $\quad f(x)=(x+2)^{2}+4$
I. $f(x)=3 x^{2}-5$
n. $f(x)=2(x-4)^{2}+3$
o. $f(x)=\frac{1}{3}(x-5)^{2}$

