

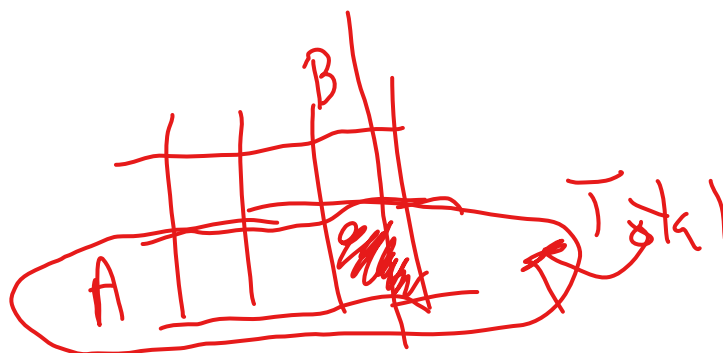
Given the points  $P(2, -1)$  and  $Q(-9, -6)$ , what are the coordinates of the point on the directed line segment  $\overline{PQ}$  that partitions  $\overline{PQ}$  in the ratio 3:2.

A.  $\left(-\frac{23}{5}, -4\right)$

B.  $\left(-\frac{12}{5}, -3\right)$

C.  $\left(\frac{5}{3}, \frac{8}{3}\right)$

D.  $\left(-\frac{5}{3}, \frac{8}{3}\right)$



## Conditional Probability

- Conditional Probability contains a condition that may limit the sample space for an event.
- You can write a conditional probability using the notation

$$P(B|A)$$

- This reads "the probability of event B, given event A"

## Conditional Probability

Ex. 1 The table shows the results of a class survey.

Find  $P(\text{own a pet} \mid \text{female})$

Given

Do you own a pet?

	yes	no	
female	8	6	14
male	5	7	12
	13	13	26

$$\frac{8 \text{ own a pet}}{14 \text{ females}} = \frac{4}{7} \text{ or } 0.57$$

## Conditional Probability

Ex. 2 The table shows the results of a class survey.

Find  $P(\text{wash the dishes} \mid \text{male})$  *denominator*

Did you wash the dishes last night?

	yes	no	
female	7	6	13
male	7	8	15
	14	14	28

$$P(\text{yes} \mid \text{male}) = \frac{\text{male and yes}}{\text{male}} = \frac{7}{15} \text{ or } .47$$

### Let's Try One

Using the data in the table, find the probability that a sample of not recycled waste was plastic.

$P(\text{plastic} \mid \text{non-recycled})$

$$\frac{P(\text{plastic} \cap \text{non-recycled})}{P(\text{non-recycled})} = P(\text{plastic} \mid \text{non-recycled})$$

$$\frac{20.4}{156.3} = .1305$$

Material	Recycled	Not Recycled
Paper	34.9	48.9
Metal	6.5	10.1
Glass	2.9	9.1
Plastic	1.1	20.4
Other	15.3	67.8

The probability that the non-recycled waste was plastic is about 13.05 %.

about 13 %

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## Conditional Probability Formula

- For any two events A and B from a sample space with  $P(A)$  does not equal zero

$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$

*A given B = over by  
B*

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## Conditional Probability

Researchers asked people who exercise regularly whether they jog or walk. Fifty-eight percent of the respondents were male. Twenty percent of all respondents were males who said they jog. Find the probability that a person randomly selected jogs given they are male.

$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$

$$P(\text{male}) = .58$$

$$P(\text{male} \cap \text{jog}) = .2$$

$$P(J|M) = \frac{P(M \cap J)}{P(M)} = \frac{.2}{.58} = .34$$

The probability that a male respondent jogs is about 34%.

## Conditional Probability – Pets Revisited

The table shows the results of a class survey.

Find  $P(\text{own a pet} \mid \text{female}) = \frac{P(\text{own} \cap F)}{P(F)} = \frac{8}{14} = \frac{4}{7} \approx .57$

Do you own a pet?

	yes	no	
female	8	6	14
male	6	7	13
			27

$$\frac{8/27}{14/27} = \frac{8}{14} = \frac{4}{7}$$

Therefore,  $P(\text{own a pet} \mid \text{female})$  equals 57%.



GSE Geometry

Unit 6 - Probability

Name: \_\_\_\_\_ Date: \_\_\_\_\_

### The Conditional Probability from Tables

The frequencies of the marbles in a bag are shown in the table.

	GREEN	BLUE	
LARGE	2	4	6
SMALL	8	12	20
	10	16	26

1. Find  $P(\text{small})$   
 $\frac{20}{26} = \frac{10}{13}$
2. Find  $P(\text{green} | \text{large})$   
 $\frac{2}{6} = \frac{1}{3}$
- Handwritten notes: "overlap green & large" and "denominator" with arrows pointing to the 2 and 6 in the fraction.*

A town planning committee is considering a new system for public transit. Residents of the town were randomly selected to answer two questions: "Do you work less than 5 miles from home?" and "Would you use the new system to get to work, if it were available?" The results are shown in the table below.

		Work less than 5 miles from home?	
		YES	NO
Use new system?	YES	24	32
	NO	44	20

3. If residents work less than 5 miles from home, what is the probability that they would use the new system?  
 $\frac{24}{68}$
4. If residents are willing to use the new system, what is the probability that they don't work less than 5 miles from home?  
 $\frac{32}{56}$
- Handwritten notes: "Conditional Given... IF... of..." and "56" and "68" with arrows pointing to the denominators in the fractions.*

The table shows the results of a poll of randomly selected high school students who were asked if they prefer to hear all school announcements in the morning or afternoon.

	Underclassmen	Upperclassmen
Morning	8	14
Afternoon	18	10

5. Find  $P(\text{Morning} | \text{Underclassmen})$   
 $\frac{8}{26}$
6. Find  $P(\text{Afternoon} | \text{Upperclassmen})$   
 $\frac{10}{24}$
- Handwritten note: "26" with an arrow pointing to the denominator in the first fraction.*

GSE Geometry

Unit 6 - Probability

The table shows the results of a customer satisfaction survey for a cellular service provider, by location of the customer. In the survey, customers were asked whether they would recommend a plan with the provider to a friend.

\_\_\_\_\_ 7. Find  $P(\text{Yes})$

\_\_\_\_\_ 8. Find  $P(\text{Yes} | \text{Arlington})$

\_\_\_\_\_ 9. Are the 2 probabilities independent?

	Arlington	Towson	Parkville
Yes	40	35	41
No	18	10	6

Roberto is the owner of a car dealership. He is assessing the success rates of his top three sales people in order to offer one of them a promotion. Over two months, for each attempted sale, he records whether the sales person made a successful sale or not. The results are shown in the cart below.

\_\_\_\_\_ 10. Find  $P(\text{Successful} | \text{Becky})$

\_\_\_\_\_ 11. Find  $P(\text{Unsuccessful} | \text{Darrell})$

	Successful	Unsuccessful
Becky	6	6
Raul	4	5
Darrell	6	9

### Conditional Probability Equations

$$P(A \cap B) = P(A) \cdot P(B | A)$$

$$P(B | A) = \frac{P(A \cap B)}{P(A)}$$

12. For two events S and Q, it is known that  $P(Q) = 0.45$  and  $P(S \cap Q) = 0.32$ . Find  $P(S | Q) = \frac{0.32}{0.45} = .71$

13. For two events B and C, it is known that  $P(C | B) = 0.61$  and  $P(C \cap B) = 0.48$ . Find  $P(B) = \frac{0.48}{0.61} = .79$

14. For two events V and W, it is known that  $P(W) = 2/9$  and  $P(V | W) = 5/11$ . Find  $P(V \cap W) = P(W) \cdot P(V | W) = (2/9)(5/11) = 10/99$

15. For two events G and H, it is known that  $P(H | G) = 5/14$  and  $P(H \cap G) = 1/3$ . Explain why you can't determine the value of  $P(H)$ .

$$P(H) = \frac{P(H \cap G)}{P(G | H)}$$

$$P(H | G) = \frac{P(H \cap G)}{P(G)} \Rightarrow P(H \cap G) = P(H | G) \cdot P(G)$$

$$P(G) = \frac{P(H \cap G)}{P(H | G)} = \frac{1/3}{5/14} = 14/15$$

We are not given  $P(G | H)$  so we cannot find  $P(H)$ .

$$P(C | B) = \frac{P(C \cap B)}{P(B)}$$

$$P(B) = \frac{P(C \cap B)}{P(C | B)}$$

$$= \frac{.48}{.61}$$

