A purple rectangular background with a white rectangular box in the center. The box has a black border and contains the text "Unit 1 Transformations in the Coordinate Plane".

# Unit 1

# Transformations

in the Coordinate Plane

# Translations

Follow the rules

Translate  $(x - 9, y + 8)$

left 9      up 8

$$C(-9, 12) \quad C'(-18, 20)$$

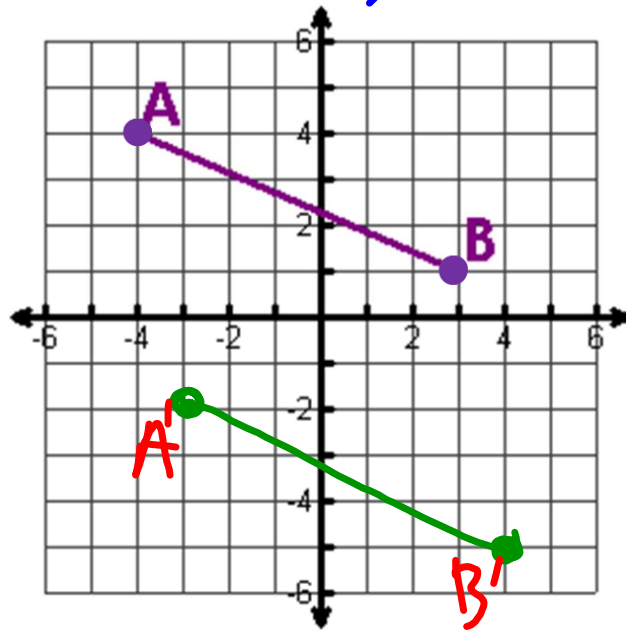
$$O(-12, -4) \quad O'(-21, 4)$$

$$W(22, -19) \quad W'(13, -11)$$

Translate  $(x + 1, y - 6)$

right 1, down 6

$$A(-4, 4)$$
$$A'(-3, -2)$$



# Reflections

Reflect across the x-axis

$$(x, y) \rightarrow (x, -y)$$

**Change the sign of the y-value**

change y

Reflect across the x-axis

$$D(-2, 4)$$

$$D'(-2, -4)$$

$$I(0, -8)$$

$$I'(0, 8)$$

$$G(-3, 5)$$

$$G'(-3, -5)$$

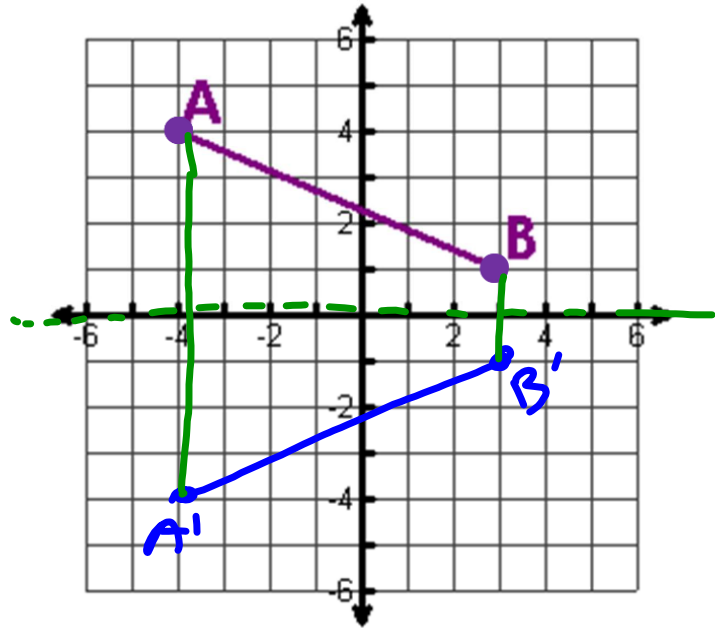
Reflect across the x-axis

$$A(-4, 4)$$

$$A'(-4, -4)$$

$$B(3, +1)$$

$$B'(3, -1)$$



**Reflect across the y-axis**

$$(x, y) \rightarrow (-x, y)$$

**Change the sign of the x-value**



change x

Reflect across the y-axis

$C(1,2)$

$C'(-1,2)$

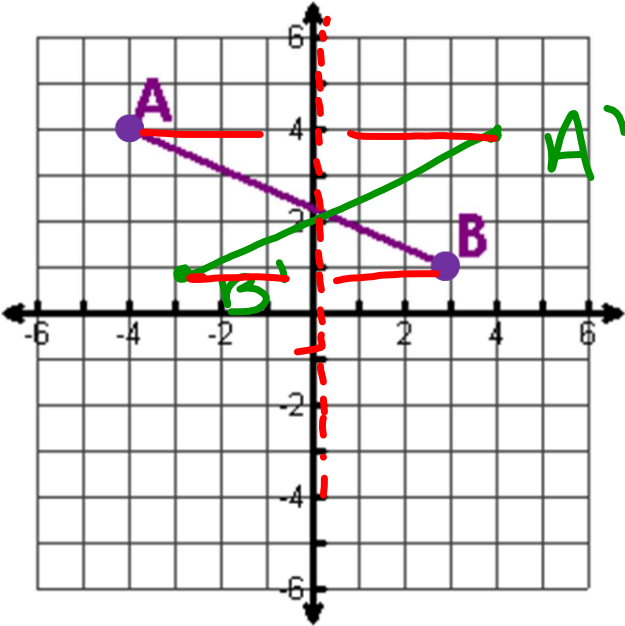
$A(-3,-5)$

$A'(3,-5)$

$T(4,-1)$

$T'(-4,-1)$

Reflect across the y-axis



**Reflect across  $y = x$**

$$(x, y) \rightarrow (y, x)$$

**Swap x and y**

Switch  $x$  &  $y$

Reflect across  $y = x$

$$B(-7, -12)$$

$$B'(-12, -7)$$

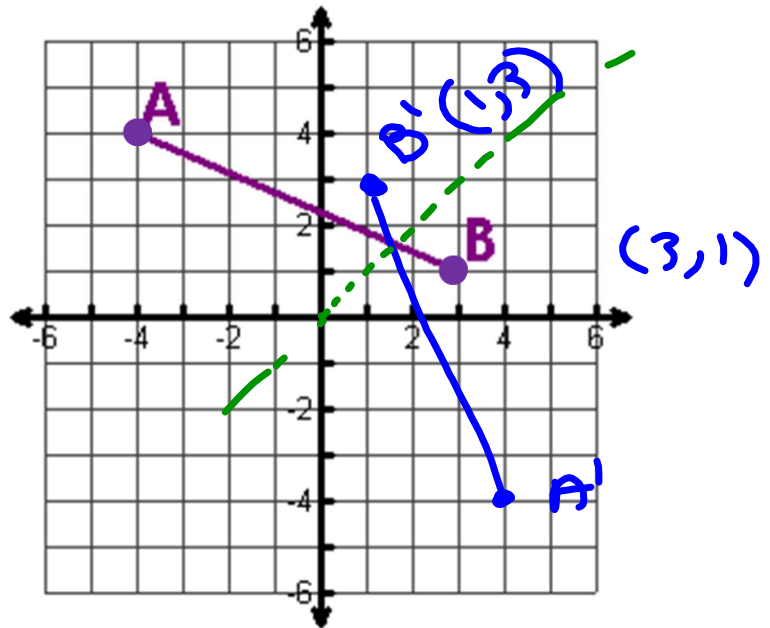
$$I(8, -2)$$

$$I'(-2, 8)$$

$$G(9, 13)$$

$$G'(13, 9)$$

Reflect across the  $y=x$



**Reflect across  $y = -x$**

$$(x, y) \rightarrow (-y, -x)$$

**Swap and change both signs**

Switch & change

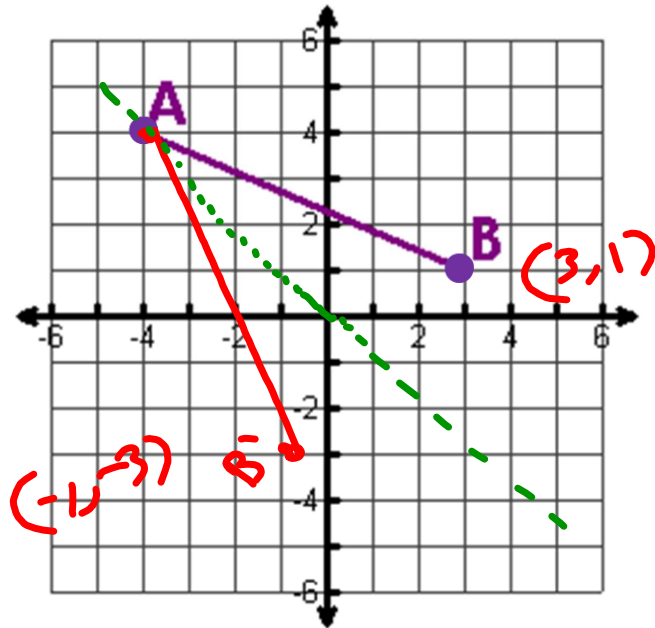
Reflect across  $y = -x$

$$M(13, 21) \quad M'(-21, -13)$$

$$A(-2, 9) \quad A'(-9, 2)$$

$$N(17, -24) \quad N'(24, -17)$$

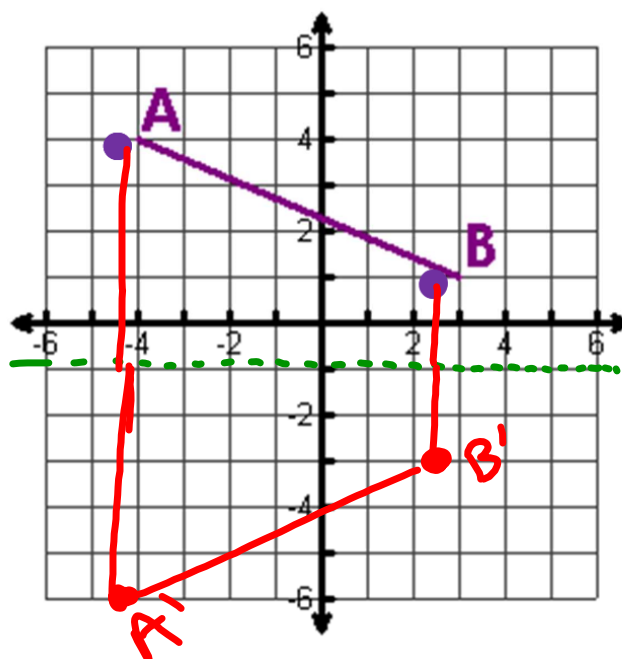
Reflect across the  $y=-x$



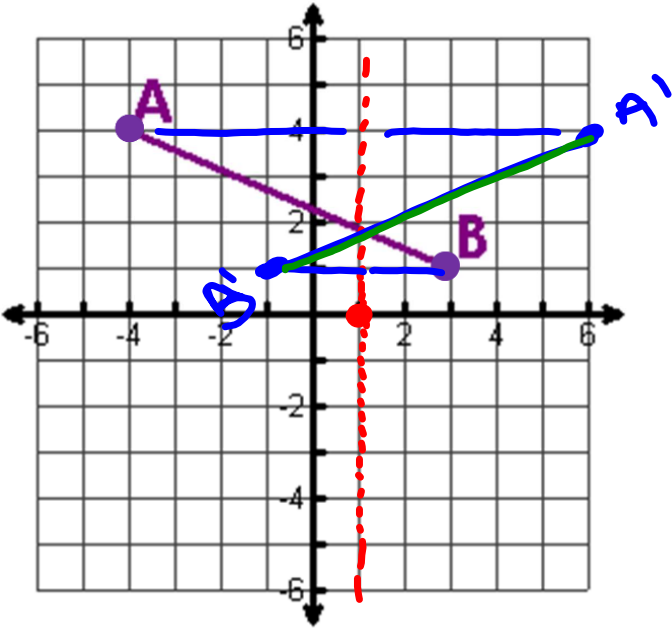


Reflect across the  $y = -1$

$$(x, 2r - y)$$



Reflect across the  $x=1$



Practice p. 24-27

10 min

Homework p. 28-29

GSE Geometry Transformations

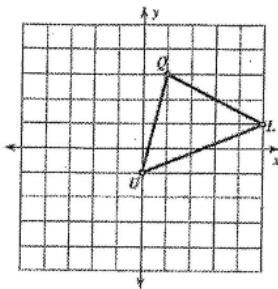
Name \_\_\_\_\_

Translations Practice

Date \_\_\_\_\_ Block \_\_\_\_\_

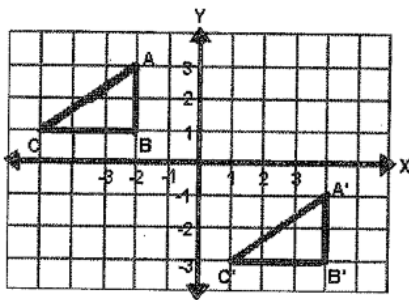
1a. Given the figure  $\triangle QUL$  shown below, translate the figure according to the following rule.

$$T(x, y) \rightarrow (x - 2, y)$$



1b. Describe in words the rule performed.

Use the following image to answer the questions below.



2a. What are the coordinates of the vertices of the pre-image?

$$A(-2, 3) \quad B(-2, 1) \quad C(-4, 1)$$

2b. What are the coordinates of the vertices of the image?

$$A'(4, -1) \quad B'(4, -3) \quad C'(0, -3)$$

2c. Explain in words how the triangle was transformed?

Shift 4 down, 6 right

2d. Write the function to describe how the triangle was transformed.

$$T(x+6, y-4)$$

Use the translation  $T(x, y) \rightarrow (x + 5, y - 9)$  for questions 3-7.

3. What is the image of  $A(-6, 3)$ ?

$$A'(-1, -6)$$

4. What is the image of  $A'$ , which would be called  $A''$ ?

$$A''(4, -15)$$

5. What is the pre-image of  $B'(12, 7)$ ?

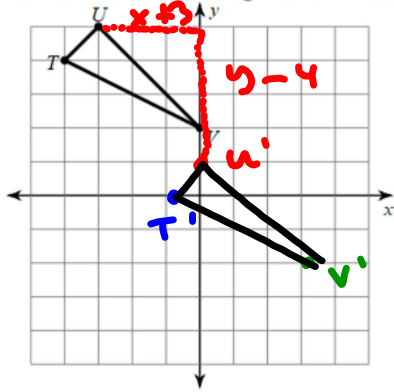
$$B(7, 16)$$

6. What is the pre-image of  $C'(-4, -8)$ ?

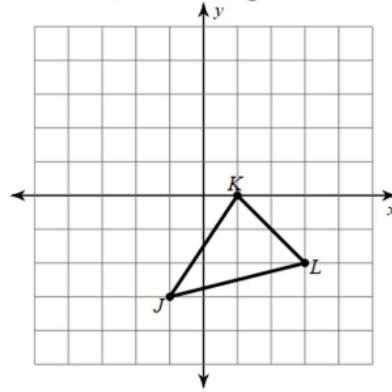
$$C(1, -1)$$

Find the coordinates of the vertices of each figure after the given transformation and graph the image.

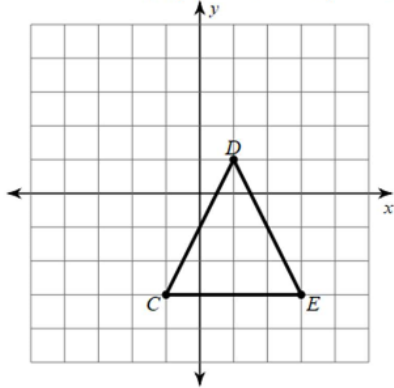
7) translation: 3 units right and 4 units down



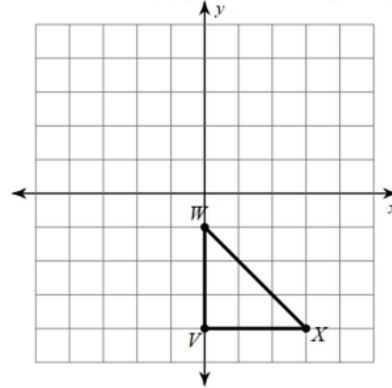
8) translation: 2 units right



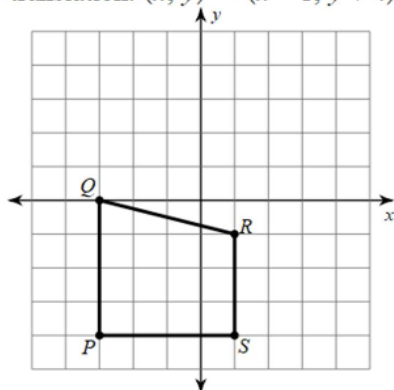
9) translation:  $(x, y) \rightarrow (x + 2, y + 2)$



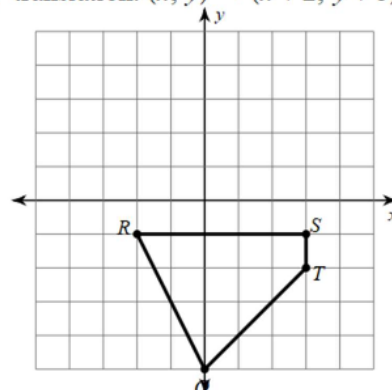
10) translation:  $(x, y) \rightarrow (x - 5, y + 1)$



11) translation:  $(x, y) \rightarrow (x - 1, y + 4)$



12) translation:  $(x, y) \rightarrow (x + 2, y + 5)$



GSE Geometry

Name \_\_\_\_\_

Reflections Practice

Date \_\_\_\_\_ Block \_\_\_\_\_

Find the coordinates of the vertices of each figure after the given transformation.

- 1) reflection across the y-axis  
 $Y(-4, 2), X(-3, 5), W(0, 4), V(-2, 1)$

- 2) reflection across  $y = -x$   
 $E(0, 0), F(-1, 4), G(1, 5), H(3, 4)$

- 3) reflection across  $y = x$   
 $T(-4, 0), U(-1, 4), V(-1, 0)$

- 4) reflection across the x-axis  
 $E(2, -1), F(1, 3), G(4, 1)$

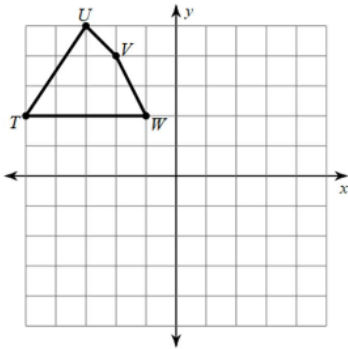
- 5) reflection across  $y = 2$   
 $K(0, 1), L(0, 3), M(5, 2), N(4, 1)$

- 6) reflection across  $x = -1$   
 $T(1, 2), U(1, 3), V(3, 3)$

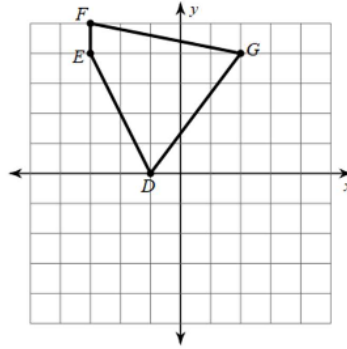
$K'(0, 3) L'(0, 1) M'(5, 2) N'(4, 3)$

Graph the image of the figure using the transformation given.

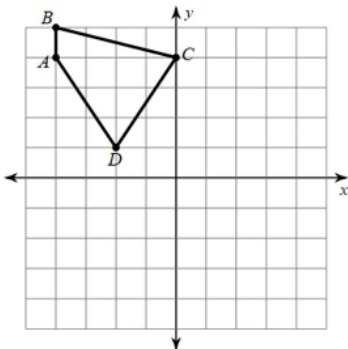
- 7) reflection across  $y = x$



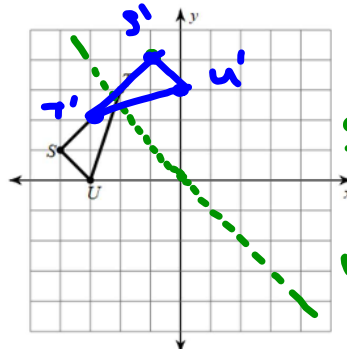
- 8) reflection across the y-axis



- 9) reflection across the x-axis

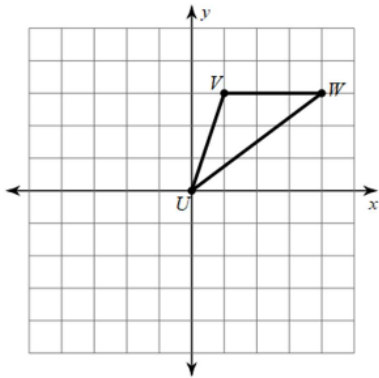


- 10) reflection across  $y = -x$

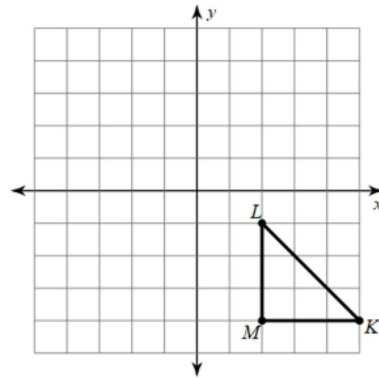


$T(-2, 3)$   
 $T'(-3, 2)$   
 $S(-4, 1)$   
 $S'(-1, 4)$   
 $u(-3, 0)$   
 $u'(0, 3)$

11) reflection across  $x = 1$

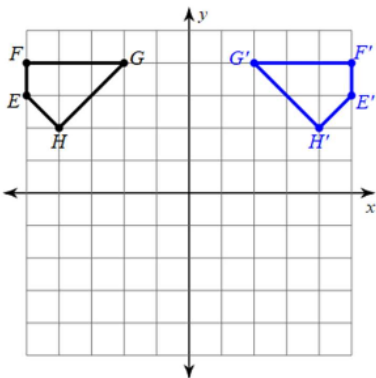


12) reflection across  $y = -1$

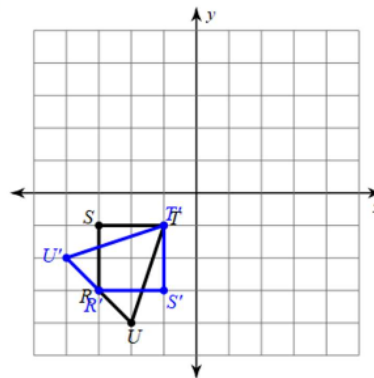


Write a rule to describe each transformation.

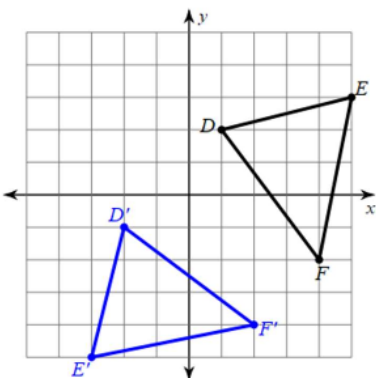
13)



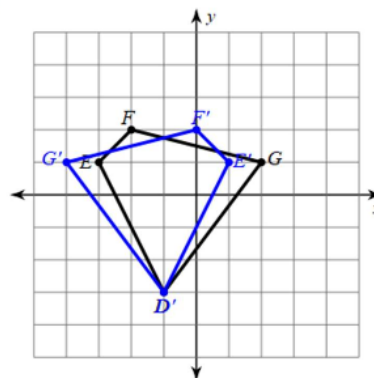
14)



15)



16)



GSE Geometry

Name: \_\_\_\_\_ Date: \_\_\_\_\_

**Translations and Reflections Homework**

1. Use the translation  $(x, y) \rightarrow (x + 5, y - 9)$  for questions a-e.

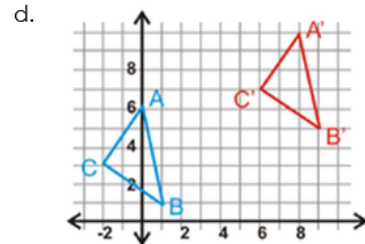
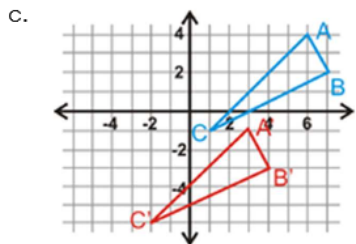
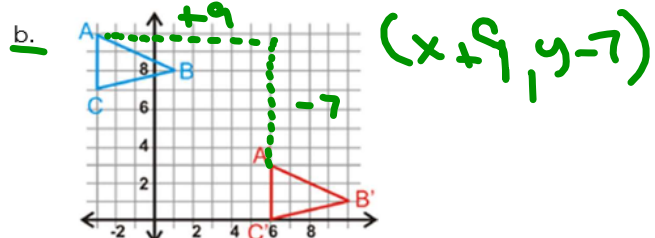
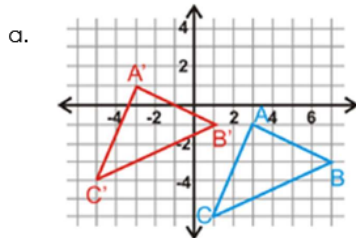
- a. What is the image of A  $(-6, 3)$ ?
- b. What is the image of  $(4, 8)$ ?
- c. What is the image of  $(5, -3)$ ?
- d. What is the pre-image of  $D'(12, 7)$ ?

2. The vertices of  $\triangle ABC$  are  $A(-6, -7)$ ,  $B(-3, -1)$ , and  $C(-5, 2)$ . Find the vertices of  $\triangle A'B'C'$ , given the translation rules below.

- a.  $(x, y) \rightarrow (x - 2, y - 7)$
- b.  $(x, y) \rightarrow (x + 11, y + 4)$
- c.  $(x, y) \rightarrow (x, y - 3)$
- d.  $(x, y) \rightarrow (x - 5, y + 8)$

$A'(5, -3)$   $B'(8, 3)$   $C'(6, 6)$

3.  $\triangle A'B'C'$  is the image of  $\triangle ABC$ . Write the translation rule for each of the following.



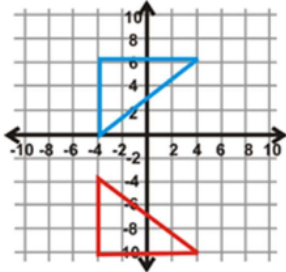
Adapted from: [Mathematics Vision Project](#)



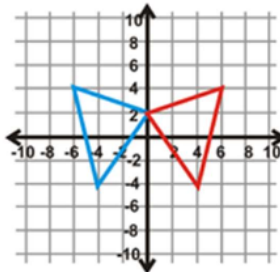
GSE Geometry

4. Find the line of reflection between the pre-image and the image.

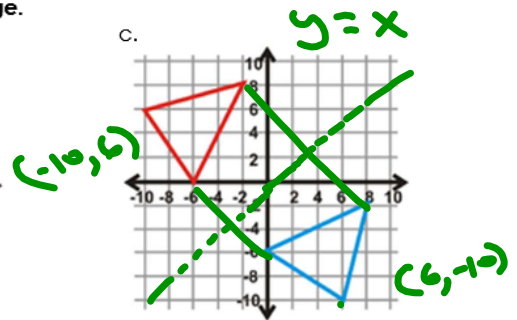
a.



b.

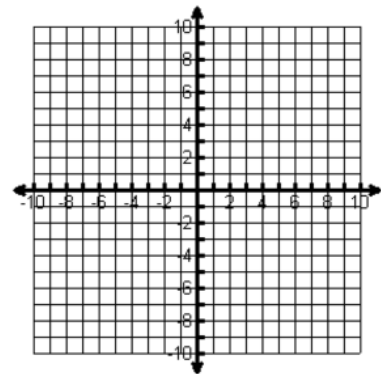


c.



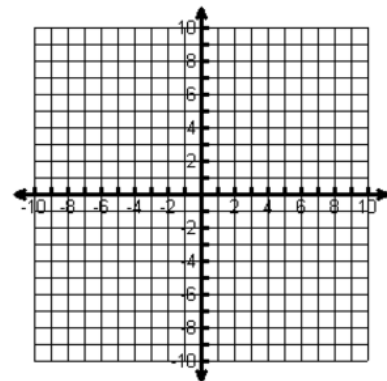
5. Two Reflections The vertices of  $\triangle ABC$  are  $A(-5, 1)$ ,  $B(-3, 6)$ , and  $C(2, 3)$ . Use this information to answer questions a-d.

- Plot  $\triangle ABC$  on the coordinate plane.
- Reflect  $\triangle ABC$  over  $y = 1$ . Find the coordinates of  $\triangle A'B'C'$ .
- Reflect  $\triangle A'B'C'$  over  $y = -3$ . Find the coordinates of  $\triangle A''B''C''$ .
- What one transformation would be the same as this double reflection?



6. Two Reflections The vertices of  $\triangle ABC$  are  $A(6, -2)$ ,  $B(8, -4)$ , and  $C(3, -7)$ . Use this information to answer questions a-d.

- Plot  $\triangle ABC$  on the coordinate plane.
- Reflect  $\triangle ABC$  over  $x = 2$ . Find the coordinates of  $\triangle A'B'C'$ .
- Reflect  $\triangle A'B'C'$  over  $x = -4$ . Find the coordinates of  $\triangle A''B''C''$ .
- What one transformation would be the same as this double reflection?



Adapted from: [Mathematics Vision Project](#)