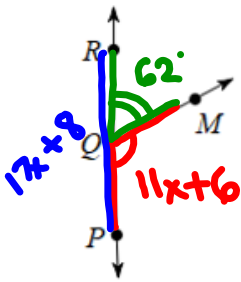


Line, Triangle, and Angle Properties

- 1) Find x if $m\angle MQP = 11x + 6$,
 $m\angle ROM = 62^\circ$, and $m\angle RQP = 17x + 8$.

We know $\angle MQP$ and $\angle RQM$
 combine to form $\angle RQP$.



$$m\angle MQP + m\angle RQM = m\angle RQP$$

$$11x + 6 + 62 = 17x + 8$$

$$\begin{array}{r} 11x + 68 \\ - 11x \end{array} \quad \begin{array}{r} = 17x + 8 \\ - 11x \end{array}$$

$$\begin{array}{r} 68 \\ - 8 \end{array} \quad \begin{array}{r} = 6x + 8 \\ - 8 \end{array}$$

$$\frac{60}{6} = \frac{6x}{6}$$

$$x = 10$$

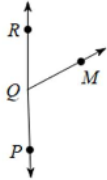
Geometry

Name _____

Line, Triangle, and Angle Properties

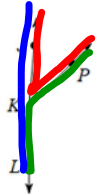
Date _____

- 1) Find x if $m\angle MQP = 11x + 6$,
 $m\angle RQM = 62^\circ$, and $m\angle RQP = 17x + 8$.



$x = 10$

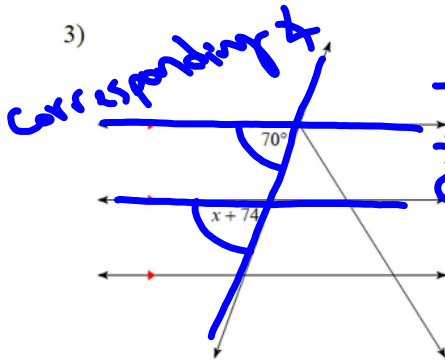
- 2) Find x if $m\angle JKP = 40x$, $m\angle PKL = 135^\circ$,
 and $m\angle JKL = 174x + 1$.



$$\begin{aligned} 40x + 135 &= 174x + 1 \\ -40x &\quad -40x \\ \hline 135 &= 134x + 1 \\ -1 &\quad -1 \\ \hline 134 &= 134x \\ x &= 1 \end{aligned}$$

Identify the property type and then solve for x .

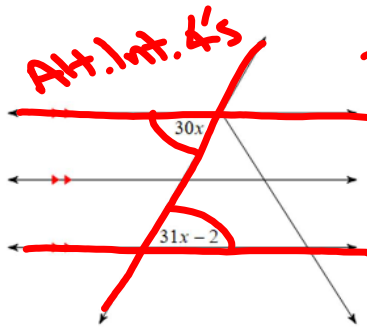
3)



Corresponding Δ 's

$$\begin{aligned} 70 &= x + 74 \\ -74 &\quad -74 \\ \hline -4 &= x \end{aligned}$$

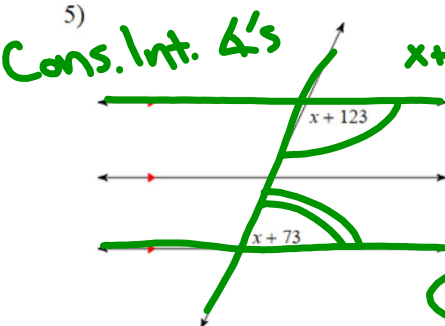
4)



Alt. Int. Δ 's

$$\begin{aligned} 30x &= 31x - 2 \\ -31x &\quad -31x \\ \hline -1x &= -2 \\ x &= 2 \end{aligned}$$

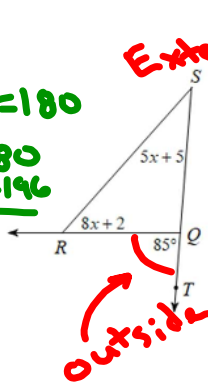
5)



Cons. Int. Δ 's

$$\begin{aligned} x + 123 + x + 73 &= 180 \\ 2x + 196 &= 180 \\ -196 &\quad -196 \\ \hline 2x &= -16 \\ \frac{2x}{2} &= \frac{-16}{2} \\ x &= -8 \end{aligned}$$

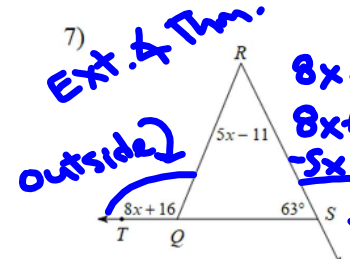
6)



Exterior Δ Thm

$$\begin{aligned} 85 &= 8x + 2 + 5x + 5 \\ 85 &= 13x + 7 \\ -7 &\quad -7 \\ \hline 78 &= 13x \\ \frac{78}{13} &= \frac{13x}{13} \\ 6 &= x \end{aligned}$$

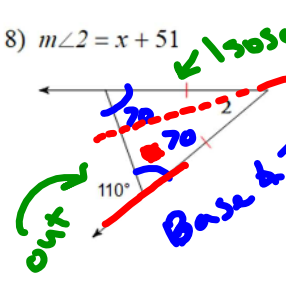
7)



Ext. Δ Thm. outside

$$\begin{aligned} 8x + 16 &= 5x - 11 + 63 \\ 8x + 16 &= 5x + 52 \\ -5x &\quad -5x \\ \hline 3x + 16 &= 52 \\ -16 &\quad -16 \\ \hline 3x &= 36 \\ \frac{3x}{3} &= \frac{36}{3} \\ x &= 12 \end{aligned}$$

8)



Linear Pair

$$\begin{aligned} 110 + \angle &= 180 \\ -110 &\quad -110 \\ \hline \angle &= 70 \end{aligned}$$

Base Δ Thm

$$\begin{aligned} x + 51 &= 40 \\ -51 &\quad -51 \\ \hline x &= -11 \end{aligned}$$

Δ Sum Thm.

$$\begin{aligned} 70 + 70 + (x + 51) &= 180 \\ 191 + x &= 180 \\ -191 &\quad -191 \\ \hline x &= -11 \end{aligned}$$

9) $m\angle 2 = x + 139$

Isosceles
Base \angle

Ext. \angle Thm.
 $m\angle 2 = 86 + 47$
 $x + 139 = 133$
 $-139 \quad -139$
 $\underline{\hspace{1cm}}$
 $X = -6$

$\frac{180}{2} = 90$
 $\frac{94}{2} = 47$

10)

Vert. \angle Thm.
 Linear Pair

Triangle Sum
 $90 + 3x + 3 + 60 = 180$
 $153 + 3x = 180$
 $-153 \quad -153$
 $\underline{\hspace{1cm}}$
 $3x = 27$
 $\frac{3x}{3} = \frac{27}{3}$
 $X = 9$

$3x + 3 = 30$

Find the value(s) of the variable(s)

11)

$y + 92 + 33 = 180$
 $y + 125 = 180$
 $-125 \quad -125$
 $\underline{\hspace{1cm}}$
 $y = 55$

$33 = 2x + 1$
 $\frac{33}{2} = \frac{2x}{2}$
 $X = 16$

12)

$4x = 48$
 $\frac{4x}{4} = \frac{48}{4}$
 $X = 12$

$y + 4(12) = 180$
 $y + 48 = 180$
 $-48 \quad -48$
 $\underline{\hspace{1cm}}$
 $y = 132$

13)

$4x = 40$
 $\frac{4x}{4} = \frac{40}{4}$
 $X = 10$

14)

$18 + 2x + 6x + 2 = 180$
 $8x + 20 = 180$
 $-20 \quad -20$
 $\underline{\hspace{1cm}}$
 $8x = 160$
 $\frac{8x}{8} = \frac{160}{8}$
 $X = 20$

$y + 27 = 180$
 $-27 \quad -27$
 $\underline{\hspace{1cm}}$
 $y = 153$

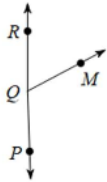
Geometry

Name _____

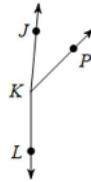
Line, Triangle, and Angle Properties

Date _____

- 1) Find x if $m\angle MQP = 11x + 6$,
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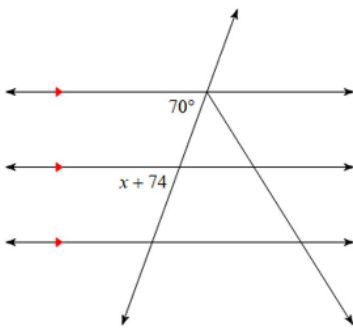


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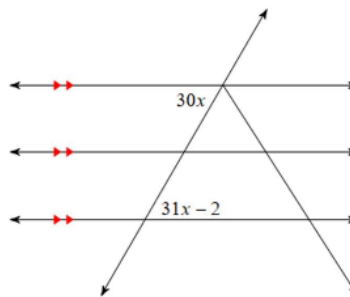


Identify the property type and then solve for x .

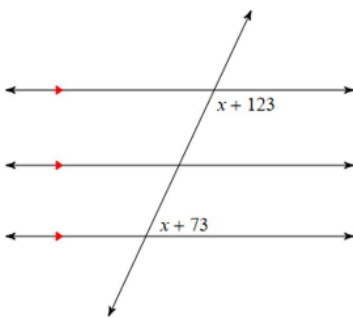
3)



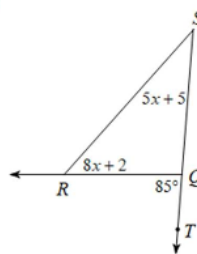
4)



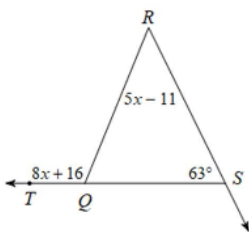
5)



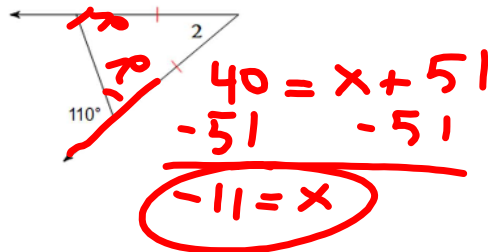
6)



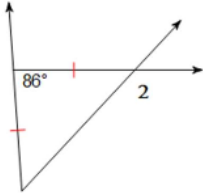
7)



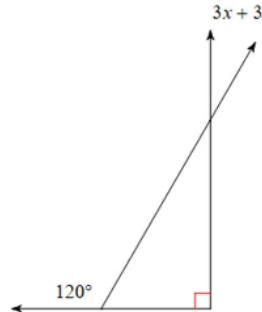
8) $m\angle 2 = x + 51$



9) $m\angle 2 = x + 139$

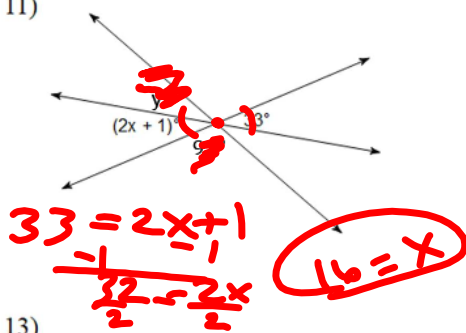


10)

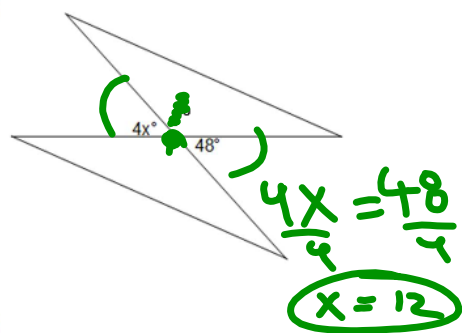


Find the value(s) of the variable(s)

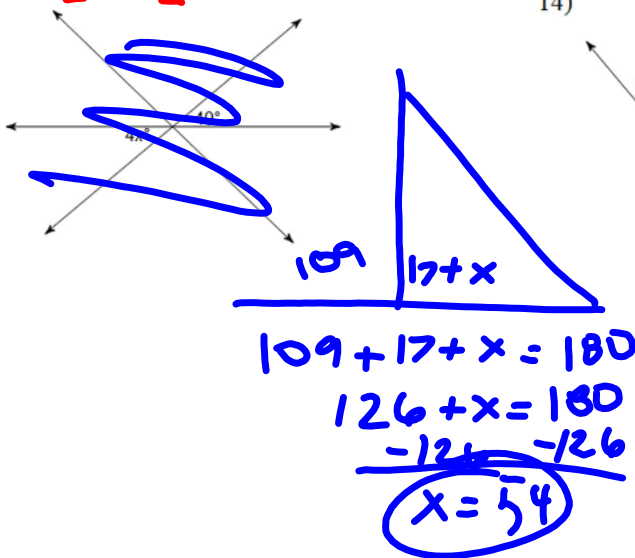
11)



12)



13)



14)

